

An improvement of dimension-free Sobolev imbeddings in r.i. spaces

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Abstract

We prove a dimension-invariant imbedding estimate for Sobolev spaces of first order, and we establish a kind of optimality.

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