

Let K be a compact Lie group (or a finite group, if one desires) and assume that K acts linearly on $W := \mathbb{R}^n$. An important question is to determine the quotient space of the K -action on W . Abstractly, the quotient space (denoted W/K) is the space of K -orbits in W and it is given the quotient topology. One can even give W/K a smooth structure by declaring that the C^∞ functions on W/K are $C^\infty(W)^K$, the K -invariant smooth functions on W . We will show that W/K is naturally (almost) an algebraic set X and that $C^\infty(W)^K \simeq C^\infty(X)$ (where we will define the latter). Finally, we will describe some results which allow one to find the equations which describe X . We will give lots of examples. One can first wonder about the case where $K = \{\pm 1\}$ acting by multiplication on \mathbb{R}^1 .